

Name: \_\_\_\_\_

Date: \_\_\_\_\_

Collaborators: \_\_\_\_\_

(Collaborators submit their individually written assignments together)

Question:	1	2	3	4	5	6	Total
Points:	10	15	10	20	20	10	85
Score:							

Instructor/grader comments:

**Course logistics**

1. (10 points) I've deleted my old homework project from my gitlab account

Sign and date here: \_\_\_\_\_

2. (15 points) I've read and understood the homework guidelines that are posted on the course website [https://www.phys.uconn.edu/~rozman/Courses/m3511\\_20s/homework.html#guidelines](https://www.phys.uconn.edu/~rozman/Courses/m3511_20s/homework.html#guidelines)

Sign and date here: \_\_\_\_\_

3. (10 points) I understand that any access to gitlab repositories of my examination projects made after the end of the exams is a case of academic misconduct

Sign and date here: \_\_\_\_\_

**Rayleigh quotient**

4. The range of the function  $R_A(\vec{x})$  is a subset of the complex plane known as the *field of values* of the matrix  $A$ .
- (a) (10 points) Write a matlab script (call it **hw01p4.m**) that use 1000 random complex vectors to plot points in the field of values of

$$A = \begin{pmatrix} 1 & 0 & -2 \\ 0 & 2 & 0 \\ -2 & 0 & 1 \end{pmatrix}$$

- (b) (5 points) continue developing your script by calculating (and printing) the eigenvalues of  $A$
- (c) (5 points) Guess (and describe below) what is the exact field of values for  $A$ .

**Similarity transformation**

5. (20 points) Recall that for the matrix

$$A = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix},$$

$$A \begin{pmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix} = \begin{pmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix}$$

and

$$A \begin{pmatrix} \frac{1}{\sqrt{2}} \\ -\frac{1}{\sqrt{2}} \end{pmatrix} = -\begin{pmatrix} \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} \end{pmatrix}.$$

Define a function of a matrix using function's Taylor series. Find  $\sin(At)$  where  $t$  is a real parameter. Show all your work.



**Gitlab**

6. (10 points) Create a gitlab project called **hw01** (name it exactly as shown). Upload **all** required matlab code and create an empty README.md file. Share the project with the instructor and the grader.