| Physics 2400 |     |    |    |       | HW 5 |
|--------------|-----|----|----|-------|------|
| Name:        |     |    |    |       |      |
| Date:        |     |    |    |       |      |
| Collaborato  | rs: |    |    |       |      |
| Question:    | 1   | 2  | 3  | Total |      |
| Points:      | 20  | 20 | 20 | 60    |      |

Instructor/grader comments:

Score:

Physics 2400 HW 5

## Method of residues

1. (20 points) Calculate the integral:

$$I = \int_{0}^{\infty} \frac{\cos(2x)}{1 + x^4} \, \mathrm{d}x.$$

Sketch the integration contour. Indicate the position(s) of the pole(s) of the integrand. Compare your answer with the result produced by a computer algebra system.

2. (20 points) Calculate the integral:

$$I = \int_0^\infty \frac{\mathrm{d}x}{1 + x^3}.$$

Use the integration contour shown in Fig. 1. Compare your answer with the result produced by a computer algebra system.

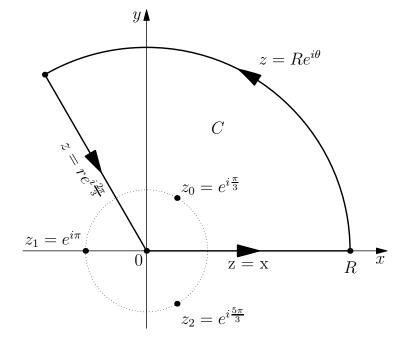


Figure 1: Integration contour for Problem 2.

3. (20 points) Calculate the integral:

$$I = \int_{0}^{\infty} \frac{\mathrm{d}x}{\left(1 + x^2\right)^2}.$$

Sketch the integration contour. Indicate the position(s) of the pole(s) of the integrand. Compare your answer with the result produced by a computer algebra system.