

## Typical Kahan Challenge (invented by J-M Müller)

“Define functions with:  $E(0) = 1$ ,  $E(z) = \frac{e^z - 1}{z}$ .  $Q[x] = \left| x - \sqrt{x^2 + 1} \right| - \frac{1}{x + \sqrt{x^2 + 1}}$ .  $H(x) = E(Q(x))^2$ .

Compute  $H(x)$  for  $x = 15.0, 16.0, 17.0, 9999.0$ . Repeat with more precision, say using BigDecimal.”

- Correct answer: (1, 1, 1, 1).
- IEEE 32-bit: (0, 0, 0, 0) **FAIL**
- IEEE 64-bit: (0, 0, 0, 0) **FAIL**
- Myth: “Getting the same answer with increased precision means the answer is correct.”
- IEEE 128-bit: (0, 0, 0, 0) **FAIL**
- Extended precision math packages: (0, 0, 0, 0) **FAIL**