

Name: _____

Date: _____

Collaborators: _____

(Collaborators submit their individually written assignments together)

Question:	1	2	3	4	5	Total
Points:	20	20	15	5	10	70
Score:						

Instructor/grader comments:

QR algorithm

1. (20 points) Write the matlab function with the following calling and return parameters

```
function [Q, R] = myqr(A)
%MYQR QR decomposition of a symmetric square matrix A
```

that implements QR decomposition of matrix A . Use the code for `hqr` and `happly` functions that we discuss in class.

Test you function using the code similar to the following.

```
n = 20;
A = gensmspectr(n);
[Q, R] = myqr(A);
norm(Q*R - A, inf)
```

The code for `gensmspectr()` is provided on the course website.

Place you testing code to the file named **hw06a.m** and submit it as a part of this assignment.

2. (20 points) Write the matlab function with the following calling and return parameters

```
function eig = myeig(A, tol)
% MYEIG Find all eigenvalues of a symmetric matrix using
%         home made implementation of QR algorithm
```

that uses QR algorithm to find all eigenvalues of a symmetric matrix. Use the code for `myqr` that you developed in Problem 1.

As you convergence test use the following

```
while err > tol
```

where

```
err = norm(diag(A, 1));
```

Compare the eigenspectrum returned by your code with the the results produced by matlab `eig` function.

```
n = 20;
A = gensmspectr(n);
```

```
e1 = myeig(A, 0.0000001);  
e2 = eig(A);  
norm(sort(e1) - sort(e2), inf)
```

Place you testing code to the file named **hw06b.m** and submit it as a part of this assignment.

3. (15 points) Use the code to investigate how the running time of your code depends on the size of the matrix n . Use matlab script similar to the following:

```
imax = 6;  
mytiming = zeros(imax, 1);  
  
for i = 1:imax  
    n = 2^i;  
    A = gensmspectr(n);  
    tol = 0.00000001;  
  
    tic();  
    e1 = myeig(A, tol);  
    mytiming(i) = toc();  
end  
  
plot(1:imax, log2(mytiming))
```

make sure you run you code several times. If the graph is (approximately) linear, determine the slope. Place the code you wrote for this part of the homework in a single matlab file, e.g. **hw06c.m**

4. (5 points) Clearly describe your observations and conclusions in your project's readme file.

Gitlab

5. (10 points) Create a gitlab project called **hw06** (name it exactly as shown). Upload **all** required matlab code and create your readme file. Share the project with the instructor.